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The ALPS Project: Open Source Software for Strongly Correlated Systems

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We present the ALPS (Algorithms and Libraries for Physics Simulations) project, an international open source software project to develop libraries and application programs for the simulation of strongly correlated quantum lattice models such as quantum magnets, lattice bosons, and strongly correlated fermion systems. Development is centered on common XML and binary data formats, on libraries to simplify and speed up code development, and on full-featured simulation programs. The programs enable non-experts to start carrying out numerical simulations by providing basic implementations of the important algorithms for quantum lattice models: classical and quantum Monte Carlo (QMC) using non-local updates, extended ensemble simulations, exact and full diagonalization (ED), as well as the density matrix renormalization group (DMRG). The software is available from our web server at http://alps.comp-phys.org/.

KEYWORDS: quantum lattice model, open source software, C++, Monte Carlo, quantum Monte Carlo, density matrix renormalization group, exact diagonalization

1. Introduction

Quantum fluctuations and competing interactions in quantum many body systems lead to unusual and exciting properties of strongly correlated materials such as quantum magnetism, $^{1)}$ high temperature superconductivity,²⁾ heavy fermion behavior,³⁾ and topological quantum order.⁴⁾ Although our understanding of these intriguing systems has grown over the past two decades, many questions remain unanswered. Strong interactions, competition between various ordered states, and strong thermal and quantum fluctuations impose limits on the applicability of mean-field theories and perturbative approaches. While renormalization group (RG) approaches can predict scaling relations in these strongly correlated regimes, the validity for realistic microscopic models of the effective actions used in the RG approaches can only be verified by numerical methods.

Direct numerical simulations of microscopic models for strongly correlated systems using unbiased and accurate algorithms are therefore of growing importance for the understanding of the unusual properties of these systems. Given the challenges faced by classical many-body simulations, such as critical slowing down and tunneling problems in classical Monte Carlo simulations, 5 it is no surprise that simulations of quantum many-body systems present even larger challenges. While the problems of critical slowing down and of tunneling through energy barriers at first order phase transitions have been

solved for bosonic and non-frustrated magnetic systems by a generalization of the classical cluster Monte Carlo^{6} and extended ensemble (broad histogram) algorithms to quantum systems, 7 the simulation of fermionic systems still presents major difficulties. Indeed, it has recently been shown that the negative sign problem of fermionic quantum Monte Carlo simulations (QMC) is NP-hard,⁸⁾ and that a general algorithm with polynomial scaling most likely does not exist. The most promising approach therefore appears to be to improve and use a variety of complementary algorithms, such as exact diagonalization,⁹⁾ series expansion¹⁰ or the density matrix renormalization group (DMRG) method.¹¹⁻¹³

The last decade has seen tremendous progress in the development of algorithms. Speedups of many orders of magnitude have been achieved.^{6, 7, 12, 13)} These advances come at the cost of substantially increased algorithmic complexity and challenge the current model of program development in this research field. In contrast to other research areas, in which large "community codes" are being used, the field of strongly correlated systems has so far been based mostly on single codes developed by individual researchers for particular projects. While the simple algorithms used a decade ago could be easily programmed by a beginning graduate student in a matter of weeks, it now takes substantially longer to master and implement the new algorithms. Thus, their use has increasingly become restricted to a small number of exJ. Phys. Soc. Jpn. Vol. 74 (2005) Supplement F. Alex et al. 31

perts.

2. The ALPS project

The ALPS (Algorithms and Libraries for Physics Simulations) project aims to overcome the problems posed by the growing complexity of algorithms and the specialization of researchers onto single algorithms through an open-source software development initiative. Its goals are to provide:

- **standardized file formats** to simplify exchange, distribution and archiving of simulation results and to achieve interoperability between codes.
- **generic and optimized libraries** for common aspects of simulations of quantum and classical lattice models, to simplify code development.
- a set of **applications** covering the major algorithms.
- **license** conditions that encourage researchers to contribute to the ALPS project by gaining scientific credit for use of their work.
- **outreach** through a web page,¹⁴⁾ mailing lists and workshops to distribute the results and to educate researchers both about the algorithms and the use of the applications.
- **improved reproducibility** of numerical results by publishing source codes used to obtain published results.
- an **archive** for simulation results.

The ready-to-use applications are useful both for *theoreticians* who want to test theoretical ideas about quantum lattice models and to explore their properties, as well as for *experimentalists* trying to fit experimental data to theoretical models to obtain information about the microscopic properties of materials.

In contrast to other fields, in which open-source development efforts began decades ago, starting now allows us to build our design directly on recent developments in computer science, in particular:

- XML¹⁵⁾ (eXtensible Markup Language) and HDF516) (Hierarchical Data Format version 5), portable data formats supported by a large number of standard tools
- generic and object oriented programming in C++ to achieve flexible but still optimal codes
- Open MP^{17} and MP^{18} for parallelization on shared memory machines and Beowulf clusters

In the following, we present additional details about these various aspects of the ALPS project.

3. File formats

The most basic part of the ALPS project is the definition of common standardized file formats suitable for a wide range of applications. Standardized file formats enable the exchange of data between applications, allow the development of common evaluation tools, simplify the application of more than one algorithm to a given model, and are a prerequisite for the storage of simulation data in a common archive.

```
<PARAMETERS>
 <PARAMETER name="LATTICE"> square </PARAMETER>
 <PARAMETER name="MODEL"> spin </PARAMETER>
 <PARAMETER name="L"> 10 </PARAMETER>
 <PARAMETER name="T"> 0.5 </PARAMETER>
</PARAMETERS>
```
Fig. 1. Excerpt from an XML file for simulation input parameters.

Fig. 2. Excerpt from an XML file for simulation results of the uniform susceptibility in a Monte Carlo simulation.

```
<LATTICEGRAPH name = "square">
  <FINITELATTICE>
    <LATTICE dimension="2"/>
    <EXTENT dimension="1" size="L"/>
    <EXTENT dimension="2" size="L"/>
    <BOUNDARY type="periodic"/>
  </FINITELATTICE>
  <UNITCELL>
    <VERTEX/>
    <EDGE>
      <SOURCE vertex="1" offset="0 0"/>
      <TARGET vertex="1" offset="0 1"/>
    </EDGE>
    <EDGE>
      <SOURCE vertex="1" offset="0 0"/>
      <TARGET vertex="1" offset="1 0"/>
    </EDGE>
  </UNITCELL>
</LATTICEGRAPH>
```
Fig. 3. The definition of a square lattice with one site (vertex) per unit cell and bonds (edges) only to nearest neighbors. First the dimension, extent, and boundary conditions of the Bravais lattice are described in the <FINITELATTICE> element, then the unit cell including the bonds in the lattice is defined.

We have designed a number of $XML \simeq 19$ to describe the input of simulation parameters, the output of results, and the specification of lattices and quantum lattice models. The ISO standard XML was chosen for the specification because it has become the main text-based data format on the internet and because it is supported by a large and growing number of tools. Unlike simple formats, in which the location of an argument in the file specifies its meaning (e.g. the first line specifies the system size, the second line temperature), XML specifies the meaning of data through meta-information provided by markup with tags, as shown in figure 1 for input parameters and figure 2 for simulation results. The meaning of these files is easy to decipher even years after completion of the simulation, unlike many other formats. The resemblance to HTML is not accidental; in fact, HTML (XHTML) is also an XML format.

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```
<BASIS name="spin">
  <SITEBASIS>
    <QUANTUMNUMBER name="S" min="1/2" max="1/2"/>
    <QUANTUMNUMBER name="Sz" min="-S" max="S"/>
    <OPERATOR name="Splus"
        matrixelement="sqrt(S*(S+1)-Sz*(Sz+1))">
      <CHANGE quantumnumber="Sz" change="1"/>
    </OPERATOR>
    <OPERATOR name="Sminus"
        matrixelement="sqrt(S*(S+1)-Sz*(Sz-1))">
      <CHANGE quantumnumber="Sz" change="-1"/>
    </OPERATOR>
    <OPERATOR name="Sz" matrixelement="Sz"/>
  </SITEBASIS>
</BASIS>
<HAMILTONIAN name="spin">
  <BASIS ref="spin"/>
  <SITETERM> -h*Sz </SITETERM>
  <BONDTERM source="i" target="j">
    Jxy/2*(Splus(i)*Sminus(j)+Sminus(i)*Splus(j))
    + Jz*Sz(i)*Sz(j)
```

```
</BONDTERM>
```

```
</HAMILTONIAN>
```
Fig. 4. The definition of a spin- $1/2$ XXZ spin Hamiltonian with one type of exchange coupling only: $H = -h\sum_i S_i^z +$ $\sum_{i,j} \left((J_{xy}/2)(S_i^+ S_j^- + S_i^- S_j^+) + J_z S_i^z S_j^z \right)$. After describing the local basis for each site and operators acting on it, the Hamiltonian is defined.

In addition to XML schemas for parameter input and for output of results, we have developed schemas for the description of lattices and models. Examples are shown in figures 3 and 4. A detailed specification of the formats is given on our XML web page.¹⁹⁾

Any of the ALPS applications can be run by providing an input file (such as the one which is excerpted in figure 1), together with lattice and model definitions (figures 3 and 4) to that application (provided the application supports that type of model). The application then returns an output file containing data such as that shown in figure 2. Standardized formats that extend across all applications reduce the learning curve for using the applications and allow common tools to be used to analyze the data.

In order to avoid working directly with the long (and sometimes ugly) output files in XML format, the XML files can be easily transformed to other formats using $XSLT$ transformations²⁰⁾ and can be viewed, for example, directly as HTML in a web browser, printed as plain text, converted to L^{AT}_EX, or displayed as a plot in one of a number of common plotting programs.21)

In addition to these text-based XML formats, the ALPS libraries support portable binary formats for large data sets such as time series of Monte Carlo simulations. These data sets are currently stored in XDR format, the standard Unix format for remote procedure calls and serialization, but plans are afoot to switch to the bettersupported HDF5 format¹⁶⁾ in the near future.

applications	OMC	ED	DMRG		
domain specific libraries	lattice	model	alea	scheduler	
numerics	random	ublas	IETL		
general C++	graph		osiris	XML	
$C/$ Fortran	BLAS		LAPACK	MPI	

Fig. 5. Hierarchical structure of the components of the ALPS project. The black frame encloses components developed as part of the ALPS project. Libraries outside the frame are publicly available high-performance libraries that can be obtained from the Boost²⁵⁾ web page or the netlib repository.²⁶⁾

4. Libraries

The ALPS libraries are the foundation of all the ALPS applications, providing functionality common to all of them:

- an XML parser and output stream to read and write the ALPS XML files.
- an expression library to manipulate and evaluate symbolic expressions.
- Monte Carlo simulations and other "embarrass-• a scheduler for the automatic parallelization of ingly" parallel applications, implementing load balancing and checkpointing.22)
- a lattice structure library for the creation of arbitrary graphs and Bravais lattices from XML input.
- a model library for the construction of basis sets, operators, and Hamiltonians from XML input.
- the "alea" library for the statistical analysis and evaluation of Monte Carlo data including a binning analysis of errors and jackknife analysis of crosscorrelations.22)
- a serialization library "osiris" for the serialization of C++ data structures, used for writing program checkpoints and portable binary result files. $^{22)}$

These libraries make full use of object-oriented and generic programming techniques, $^{23)}$ which allows them to be very flexible without losing any performance compared to FORTRAN programs. To give just one example, the lattice library, which is implemented generically using C++ template features and is based on the Boost Graph Library^{24, 25} (BGL), does not restrict the user to a specific data structure as in C or Fortran libraries. Instead, the application programmer can choose the data structure best suited for the application. As long as this data structure provides the BGL graph interface, the ALPS lattice library can construct the lattice from the XML description.

Figure 5 shows a diagrammatic overview of the hierarchy of components in the ALPS project: the ALPS applications (discussed in the next section) are based on domain-specific ALPS libraries, such as the lattice, model, alea, or the scheduler library. These libraries are based on numerical and general C++ libraries, developed either in ALPS or in the $C++$ Boost project.²⁵⁾ In addition to the BGL mentioned above, the external libraries include the Boost random number library, which

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has been accepted into the next release of the C++ standard as a standard library, and the Boost uBLAS library for matrix and vector operations. A numerical library developed by us and distributed with the ALPS software, the Iterative Eigensolver Template Library²⁷⁾ (IETL), provides a package of iterative eigensolvers for sparse matrices. Finally, the lowest level of the hierarchy is a set of common C and FORTRAN libraries, including the high performance BLAS and LAPACK libraries for linear algebra and the MPI and PVM libraries for communication on distributed systems.

5. Applications

The following application programs, based on the above libraries, are implemented in release 1.2:

- a Monte Carlo program for classical magnets employing cluster algorithms.28)
- the QMC program "looper" using the loop cluster algorithm^{6, 29)} in a stochastic series expansion³⁰⁾ (SSE) and path-integral representation for quantum magnets with spin reversal symmetry.
- an optimized directed loop QMC program31) in an SSE representation for bosonic and magnetic quantum lattice models.
- a worm algorithm32) QMC program best suited for bosonic quantum lattice models and easy-axis quantum magnets.
- an extended ensemble QMC program using a generalization of the Wang-Landau³³ algorithm to quantum systems,7) to obtain thermodynamic quantities over large temperature ranges.
- an exact diagonalization program which can calculate the ground state and low lying excited states of quantum lattice models using the Lanczos^{34} algorithm.
- a full diagonalization program which can calculate the complete eigenspectrum of quantum lattice models and from it all thermodynamic properties.
- a $DMRG^{11}$ program for *noninteracting* particles. This is an adaptation of the program in Refs.^{13, 35)} to the ALPS libraries. In addition to demonstrating the fundamental ideas of the DMRG, it solves onedimensional single-particle quantum problems in arbitrary potentials.

Planned for the future are:

- support for lattice symmetries in the exact and full diagonalization codes in release 1.3.
- a $DMRG^{11-13}$ code for static properties in release 1.3.
- \bullet a series expansion¹⁰⁾ code for both perturbation series and high temperature series.
- \bullet a determinental QMC³⁶⁾ code for two- and threedimensional fermionic models.
- a toolset for mean-field calculations on quantum lattice models.

These applications comprise the most important unbiased algorithms for quantum many body systems. The

implementations all share the same file formats, simplifying their use, reducing the learning curve, and enabling the easy investigation of a model with more than one method. Tutorials on the use of the applications are included with the sources that can be found on the ALPS web $\rm{page.}^{14)}$

These codes and libraries have already been used in a number of publications, of which we will mention only a small representative sample illustrating the breadth of possible applications. The exact diagonalization library was used in the investigation of quantum bits with topological protection.37) Anisotropic quasi-one dimensional and quasi-two dimensional quantum magnets were investigated recently using the "looper" QMC program.38) A precursor of the looper program was used for extensive fits of QMC simulations to experimental measurements^{39, 40}) and to determine phase diagrams critical exponents of quantum phase transitions 41 and universal critical temperatures of quantum critical magnets in a field.42) A precursor of the directed loop program based on the ALPS libraries has been used to determine ground state and finite-temperature phase diagrams of hard-core bosons.43) The optimized directed loop and worm algorithm QMC programs were applied to determine properties of ultra-cold bosonic atoms in optical lattices $^{44)}$ and to calculate magnetization curves of spin systems.45) The ALPS libraries were also employed recently in simulations of dissipative quantum phase transitions, 46 in a spin-wave analysis of quantum magnetic quasicrystals, 47) and in a multi-scale approach to the simulation of nanomagnets.48)

6. License and Motivations to Contribute

The ALPS library⁴⁹⁾ and application⁵⁰⁾ licenses were designed by I.P. McCulloch after extensive discussions inside the ALPS collaboration. They are based on the GNU general public license.⁵¹⁾ The use of the libraries and codes is free but carries a citation requirement to publications describing the libraries and codes.

Stricter licensing terms, such as the requirement to submit any modifications and improvements of the codes to the ALPS collaboration, or a requirement to publish any codes built on the ALPS libraries or applications as a supplement to the paper presenting the results, were discussed but have not been included in the license at the present time. We feel, however, that the idea of publishing source code of numerical simulations together with the scientific results produced could be very beneficial by enabling reproducibility of numerical simulations. We encourage a wider discussion on this question in the computational physics community.

Besides "payment" in the scientific currency of citations, and peer pressure to contribute after profiting from the ALPS project, additional motivations (especially for junior researchers) to contribute to the ALPS project are networking opportunities and many chances to start new research collaborations based on codes contributed to the ALPS project.

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7. Outreach and Development

The ALPS web $page¹⁴$ is the central information repository of the ALPS collaboration. It makes source codes of the ALPS libraries and applications available, provides access to the documentation, and distributes information about the mailing lists, new releases, and workshops.

We intend to provide extensive tutorials with handson sessions using the ALPS applications at workshops on numerical simulations of quantum lattice models at least once per year. Such tutorials have thus far been held on three occasions: a workshop on Wang-Landau sampling for classical and quantum systems at Oak Ridge National Labs in August 2003, a graduate lecture series at the University of Hannover, Germany in November 2003, and a workshop on simulation tools in Lugano, Switzerland in September 2004.52) More tutorials are planned for 2005 and 2006.

The ALPS project has been further publicized by talks, such as an invited talk by S. Trebst at the 2004 March Meeting of the American Physical Society,⁵³⁾ a presentation at the DMRG workshop at the Lorentz center in Leiden, 54 and poster presentations at various conferences.

Development of the ALPS libraries and applications is coordinated through both mailing lists and semi-annual developer workshops. These ALPS developer workshops (all held in alpine regions so far) have been instrumental not only in planning development efforts for the subsequent half year, but also in providing important development deadlines – and thus counter the susceptibility of all software projects to interminable delays.

8. Future plans

The ALPS project is continuously evolving; many improvements and additions are planned for forthcoming releases. Planned near-term improvements, in addition to those mentioned in section 5 will be the capability of specifying arbitrary measurements of local operators and correlation functions in input files.

A major future development effort will be to establish a database and archive for simulation results based on our proposed XML formats. Whereas today simulation results are usually published only in the form of figures or fit results after much data processing, the archive will allow the easy retrieval of detailed results in a unified format. Current research on data and storage grids as well as the rapid progress in the development of XMLbased databases and tools will surely prove helpful for this project.

In a further stage, we envision expanding the ALPS project in the long term to include dynamical mean field theory (DMFT) codes⁵⁵⁾ as well as interfacing the ALPS applications to band structure codes, thus making it possible to obtain a microscopic lattice model from ab-initio calculations. These efforts will be coordinated with the ψ -Mag project at Oak Ridge National Laboratory, which aims at unifying the interface of band structure codes and at combining them with classical spin dynamics simulations for nanomagnetics.⁵⁶⁾

In addition to these coordinated development efforts, we offer a repository for other open source simulation codes on our computational physics web page http://www.comp-phys.org/.

9. Conclusions

The ALPS project is an open source effort at providing libraries and applications for the simulation of classical and quantum lattice models. Common XML file formats enable the sharing and archiving of simulation data. Generic and optimized libraries simplify the development of simulation codes by implementing common tasks such as I/O and the construction of lattice and model data structures. The ALPS applications make modern highperformance numerical algorithms available to a wider range of researchers. They enable theoreticians to investigate properties of interesting strongly correlated models conveniently, and allow experimentalists to perform direct comparisons and fits of experimental measurements to numerical simulations.

Researchers interested in announcements of new releases, information about workshops, or in contributing to the ALPS project are encouraged to sign up to the mailing lists on our web page. $^{14)}$

History and Acknowledgment

The ALPS project was formally initiated at a workshop in Guarda, Switzerland in January $2003,57$ by merging the PALM++ library²²⁾ for distributed Monte Carlo simulations and projects based on it, the opensource Looper²⁹ code, and the IETL library for sparse eigensolvers,27) with development efforts on DMRG and other algorithms.

The initial idea for the project was seeded by D.C. Johnston (Ames Laboratory), who in the course of fruitful collaborations on fitting experimental measurements on quasi-one dimensional systems to QMC simulations,39) demonstrated the usefulness of computational algorithms for experimental physicists. Additional motivation came from our desire to ease the exchange of codes in research collaborations, and by the ψ -Mag project at Oak Ridge National Laboratories.⁵⁶⁾

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